

Neving

Trigonometry:

Formulae

$$1. \operatorname{Cosec} \theta = \frac{1}{\sin \theta}$$

$$2. \sec \theta = \frac{1}{\cos \theta}$$

$$3. \cot \theta = \frac{1}{\tan \theta} = \frac{\cos \theta}{\sin \theta}$$

$$4. \tan \theta = \frac{1}{\cot \theta} = \frac{\sin \theta}{\cos \theta}$$

$$5. \sin^2 \theta + \cos^2 \theta = 1.$$

$$6. \sec^2 \theta = 1 + \tan^2 \theta$$

$$7. \operatorname{Cosec}^2 \theta = 1 + \cot^2 \theta$$

θ	$0^\circ = 0^\circ$	$30^\circ = \frac{\pi}{6}$	$45^\circ = \frac{\pi}{4}$	$60^\circ = \frac{\pi}{3}$	$90^\circ = \frac{\pi}{2}$
$\sin \theta$	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1
$\cos \theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0
$\tan \theta$	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	∞

$$* \sin 2\theta = 2 \sin \theta \cos \theta$$

$$* \cos 2\theta = \cos^2 \theta - \sin^2 \theta = 2 \cos^2 \theta - 1 = 1 - 2 \sin^2 \theta$$

9. Maximum value of $\sin \theta$, $-\sin \theta$, $\cos \theta$, $-\cos \theta$ is 1.

10. Minimum value of $\sin \theta$, $-\sin \theta$, $\cos \theta$, $-\cos \theta$ is -1.

11(a). Maximum value of $\sin^2 \theta$ and $\cos^2 \theta$ is 1.

(b). Minimum value of $\sin^2 \theta$ and $\cos^2 \theta$ is 0 (zero).

12(a). Maximum value of $-\sin^2 \theta$ and $-\cos^2 \theta$ is 0 (zero).

(b). Minimum value of $-\sin^2 \theta$ and $-\cos^2 \theta$ is -1.

13. For $x \in \mathbb{R}$, the range of $\sin x$, $\cos x$, $-\sin x$, $-\cos x$ is $-1 \leq f(x) \leq 1$.

$$14. f(x) = a + b \cos x, \quad g(x) = a - b \cos x = a + b(-\cos x)$$

$$h(x) = a + b \sin x, \quad m(x) = a - b \sin x = a + b(-\sin x).$$

(a)(i) Maximum value of $f(x)$, $g(x)$, $h(x)$ and $m(x)$ is $(a+b)$.

(ii) Minimum value of $f(x)$, $g(x)$, $h(x)$ and $m(x)$ is $(a-b)$.

(b) Amplitude of $f(x)$, $g(x)$, $h(x)$ and $m(x)$ is b .

15.(a). Period of $\sin x$, $-\sin x$, $\cos x$, $-\cos x$ is 360° and
Period of $\tan x$ is 180° .

(b). Period of $\sin ax$, $\cos ax$, $-\sin ax$, $-\cos ax$ is $\frac{360^\circ}{a}$.
and period of $\tan ax$ is $\frac{180^\circ}{a}$.