

$$p^2 + 10p + 5^2 = 4200 + 5^2$$

$$(p+5)^2 = 4225$$

$p+5 = \sqrt{4225}$; disregard the negative root since p is a positive value.

$$p+5=65$$

$$p= 65-5$$

$p= 60$; substitute this to supply function to get q

$$q=2p-30$$

$$= 2(60)-30$$

$$= 120-30$$

$$q= 90$$

Substitute q in demand function:

$$(p+10)(90-30)=8400$$

$$(p+10)(60)=8400$$

$$60p+600=8400$$

$$p= (8400-600)/60$$

$$p= 130$$

For equilibrium price ;

$$q_s=q_d$$

$$2p-30= (8400/p+10)-30$$

$$2p(p+10)=8400$$

$$2p^2+20p-8400= 0$$
 ; find the root, only take the positive root.

$$p^2+10p+5^2= 4200+5^2$$
 ; as we have get earlier $p= \$65$ is the equilibrium price

For the equilibrium quantity;

$$p_s=p_d$$

$$q/2 +15 = (8400/q+30)-10$$

$$q/2+25 = 8400/q+30$$

$$q/2(q+30)+25(q+30)= 8400$$

$$q^2/2 +15q +25q+ 750-8400 =0$$

$$q^2/2 +40q -7650 =0$$
 ; multiply by 2 to eliminate fraction

$$q^2+80q-15300=0$$
 ; find the roots and take the positive root only

$$q^2+80q+40^2=15300+40^2$$

$$(q+40)^2=16900$$

$$q +40 =\sqrt{16900}$$

$$q = 130-40$$

$$q = 90, \text{ is the equilibrium quantity}$$

The market equilibrium point (q,p)

$$(90,65)$$