

Решение:

Бидејќи секој шахист одиграл со секого по една партија, тука станува збор за комбинации. Притоа непознат е вкупниот број на учесници n , но познато е дека $C_n^2 = 45$

$$\frac{n!}{(n-2)! \cdot 2!} = \frac{n(n-1)}{2 \cdot 1} = 45$$

$$n(n-1) = 90$$

$$n^2 - n - 90 = 0$$

$$n_{1,2} = \frac{1 \pm \sqrt{1+360}}{2} = \frac{1 \pm 19}{2}$$

го отфрламе негативното решение

$$n = 10$$

На турнирот имало 10 учесници.

Set of elementary events. Random events.

Problem 1. An experiment consists of throwing a dice. Describe the set of elementary events and the following random events:

A: an even number is observed,

B: a number divisible by 3 is observed,

C: a number smaller than 5 is observed.

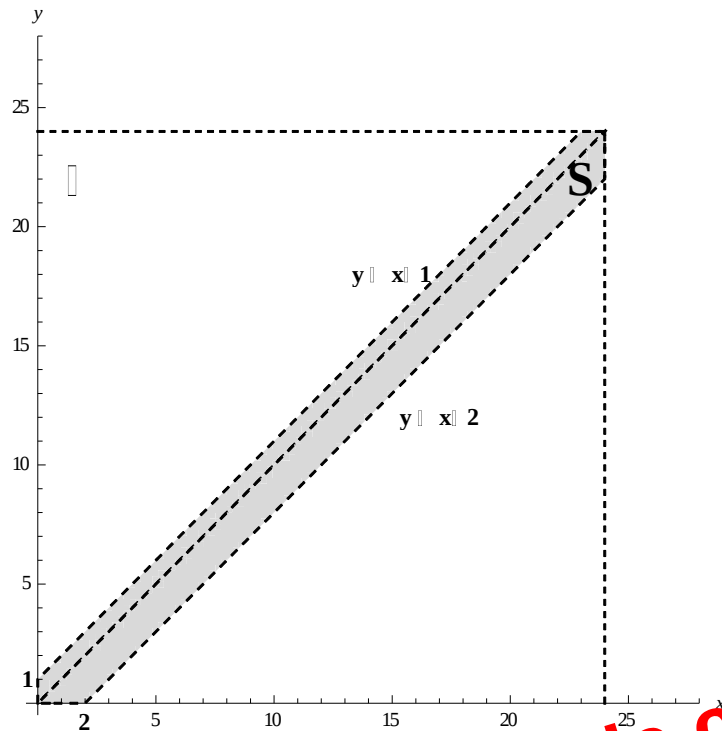
Solution: Let the elementary event E_i denote that we observe the number i when throwing the dice $i=1,2,\dots,6$. Then, the set of elementary events Ω is given by $\Omega=\{E_1, E_2, E_3, E_4, E_5, E_6\}$, and

$$A=\{E_2, E_4, E_6\},$$

$$B=\{E_3, E_6\},$$

$$C=\{E_1, E_2, E_3, E_4\}$$

Problem 2. One box contains 4 pieces of paper, numerated with the numbers 1,2,3 and 4. At random we take a paper from the box without returning, until an odd number is drawn. Find the set of elementary events and the following events:



$$m(\Omega) = 24 \cdot 24 = 576$$

$$m(S) = 24 \cdot 24 - \left(\frac{23 \cdot 23}{2} + \frac{22 \cdot 22}{2} \right) = 64.5$$

The probability that the event S will happen is:

$$P(S) = \frac{m(S)}{m(\Omega)} = 0.12.$$

Problem 2. Find the probability that the sum of two randomly chosen positive numbers smaller than 1 will be smaller than 1, and that their product will be less than $2/9$.

Solution:

$$\Omega = \{(x, y) \mid 0 \leq x, y \leq 1\}, \quad m(\Omega) = 1$$

$$S = \{(x, y) \mid 0 < x, y < 1, x + y < 1, xy < 2/9\}$$