

Eliminating left recursion

- An algorithm to eliminate arbitrary left recursion (by replacing it with right recursion) is as follows:
 1. Arbitrarily order the non-terminals: N_1, N_2, N_3, \dots
 2. Apply the following steps to the productions for N_1 , then N_2 , ...
 3. For N_i :
 - a) For all productions $N_i \rightarrow N_k \alpha$, where $k < i$ and if the productions for N_k are $N_k \rightarrow \beta_1 \mid \beta_2 \mid \beta_3 \mid \dots$ then expand the reference to N_k , i.e. replace the production $N_i \rightarrow N_k \alpha$ by $N_i \rightarrow \beta_1 \alpha \mid \beta_2 \alpha \mid \dots$
 - b) If the productions for N_i are now

$$N_i \rightarrow \alpha_1 \mid \alpha_2 \mid \dots \mid N_i \beta_1 \mid N_i \beta_2 \mid \dots$$
 (where the first few are not left recursive while the latter are) then replace them with

$$N_i \rightarrow \alpha_1 N_i' \mid \alpha_2 N_i' \mid \dots$$

$$N_i' \rightarrow \epsilon \mid \beta_1 N_i' \mid \beta_2 N_i' \mid \dots$$

Example of eliminating left recursion

- Consider the productions:

$$A \rightarrow a \mid Ba \quad B \rightarrow b \mid Cb \quad C \rightarrow c \mid Ac$$
 1. Arbitrarily order the non-terminals: A, B, C
 2. Consider the productions for A: no change
 2. Consider the productions for B: no change
 3. Consider the productions for C:
 - a) Replace $C \rightarrow Ac$ by $C \rightarrow ac \mid Bac$
 - a) Replace $C \rightarrow Bac$ by $C \rightarrow bac \mid Cbac$
 Productions for C are now: $C \rightarrow c \mid ac \mid bac \mid Cbac$
 - b) Replace the productions for C by:

$$C \rightarrow cC' \mid acC' \mid bacC'$$

$$C' \rightarrow \epsilon \mid bacC'$$

A Workable Solution

Observation

- The trouble which gives rise to nondeterminacy and backtracking in top down parsers shows itself in only one place – that is when a parser has to choose between several alternatives with the same left hand side.
- The only information which we can use to make the *correct decision* is the input stream itself.
 - In the example, we (humans) could see which alternative to choose by looking at the input yet-to-be-read.
- If we are going to *look ahead* in order to make the correct decision, we need a buffer in which to store the next few symbols.
- In practice, this buffer is of a fixed length.

Definitions

- A parser which can make a deterministic decision about which alternative to choose when faced with one, if given a buffer of k symbols, is called a $LL(k)$ parser.
 - Left to right scan of input
 - Left most derivation
 - k symbols of look-ahead
- The grammar that an $LL(k)$ parser recognizes is an $LL(k)$ grammar and any language that has an $LL(k)$ grammar is an $LL(k)$ language.
 - We are constructing an $LL(1)$ compiler that recognises $LL(1)$ grammars.
 - So the question is *How do we know when we have an $LL(1)$ grammar?*
- We also have $LR(k)$ grammars and other variations, but our focus is currently on $LL(1)$ grammars.