

- $F_x(2) = P(X \leq 2)$
- Cumulant generating function = $\psi_x(t) = \ln M_x(t)$
- $E(h(x)) = \int_{-\infty}^{\infty} h(x)f_x(x)dx$
- $E(X) = \sum_{i=1}^{\infty} x_i f_{x_i}(x)dx$ with discrete function

$$E(X) = \int_{-\infty}^{\infty} x f_x(x)dx \text{ with continuous function}$$

NB. –Boundaries depend on the definition of the function.

- Discrete distributions:

1- Uniform:

$$X \sim U^d(a, b),$$

$$p(x) = \frac{1}{n}$$

$$E(x) = \frac{a+b}{2}$$

$$\text{Var}(x) = \frac{n^2-1}{12}$$

$$M_x(t) = \frac{e^{at} - e^{(b+1)t}}{n(1-e^t)}$$

Ex: A die is tossed.

2- Binomial :

$$X \sim B(n, p), x = 0, 1, \dots$$

$$p(x) = \binom{n}{x} p^x (1-p)^{n-x}$$

$$E(x) = np$$

$$\text{Var}(x) = np(1-p)$$

$$M_x(t) = (pe^t + 1 - p)^n$$

x: number of successes in n trials.