

## Differentiation

1.  $x^n \rightarrow nx^{n-1}$

e.g.  $x^3 \rightarrow 3x^2$

2.  $x \rightarrow 1$

e.g.  $3x \rightarrow 3$

3. number  $\rightarrow 0$

e.g.  $5 \rightarrow 0$

4.  $\frac{1}{x^n} \rightarrow x^{-n}$

e.g.  $\frac{3}{x^2} \rightarrow 3x^{-2}$

example

differentiate  $y = 4x^5 + 7x + 3$

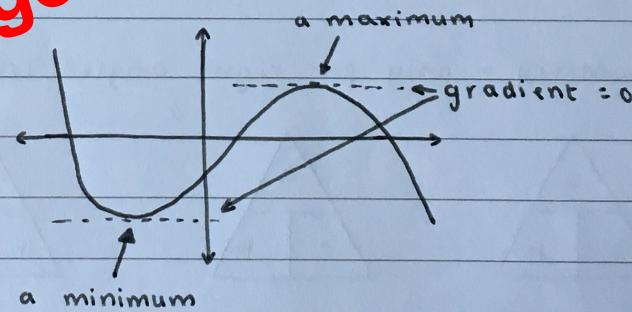
$$\frac{dy}{dx} = 20x^4 + 7$$

differentiate  $y = 7 + 6x + 3x^4 + 2 + \frac{4}{5x^3}$

$$\frac{dy}{dx} = 6 + 12x^3 + 20x^{-3}$$

Maximum and minimum

$$\frac{dy}{dx} = 0$$



- work out  $x$

- input  $x$  to work out  $y$

example

find the maximum of  $\frac{dy}{dx} = 20x - 10$

$$0 = 20x - 10$$

$$y = x^2 - 10x$$

$$\text{maximum} = (0.5, 4.9)$$

$$10 = 20x$$

$$y = 0.5^2 - (10 \times 0.5)$$

$$x = 0.5$$

$$y = -4.9$$