

CONT. by formula: $y' = u dv + v du$

$$y' = e^x (e^x \cos e^x) + \sin e^x (e^x)$$

$$y' = e^{2x} \cos e^x + e^x \sin e^x$$

⑧ $y = \frac{e^x}{x}$

let $u = e^x$

$v = x$

$du = e^x$

$dv = 1$

by formula: $y' = \frac{v du - u dv}{v^2}$

$$y' = \frac{x(e^x) - e^x(1)}{x^2}$$

$$y' = \frac{e^x(x-1)}{x^2} \quad \rightarrow e^x \text{ is factored out}$$

⑨ $y = \tan e^{\sqrt{x}}$

$$y' = \sec^2 e^{\sqrt{x}} \left[\frac{d}{dx} (e^{\sqrt{x}}) \right]$$

$$= \sec^2 e^{\sqrt{x}} (e^{\sqrt{x}}) \left[\frac{d}{dx} (\sqrt{x}) \right]$$

$$= \sec^2 e^{\sqrt{x}} (e^{\sqrt{x}}) \left(\frac{1}{2} x^{-1/2} \right)$$

$$= \frac{1}{2} x^{-1/2} e^{\sqrt{x}} \sec^2 e^{\sqrt{x}}$$

$$y' = \frac{e^{\sqrt{x}} \sec^2 e^{\sqrt{x}}}{2\sqrt{x}}$$

⑩ $y = e^{e^x}$

$$y' = e^{e^x} \left[\frac{d}{dx} (e^x) \right]$$

$$y' = e^{e^x} (e^x)$$

⑪ $y = \frac{e^x - e^{-x}}{e^x + e^{-x}}$

let $u = e^x - e^{-x}$

$v = e^x + e^{-x}$

$du = e^x - e^{-x}(-1)$

$dv = e^x + e^{-x}(-1)$

$du = e^x + e^{-x}$

$dv = e^x - e^{-x}$

by formula: $y' = \frac{u dv - v du}{v^2}$

$$y' = \frac{(e^x - e^{-x})(e^x - e^{-x}) - (e^x + e^{-x})(e^x + e^{-x})}{(e^x + e^{-x})^2}$$

$$= \frac{(e^{2x} + 2 + e^{-2x}) - (e^{2x} - 2 + e^{-2x})}{(e^x + e^{-x})^2}$$

$$y' = \frac{4}{(e^x + e^{-x})^2}$$

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