

3. Completing the Square

$$\begin{aligned}
 4x^2 - 16x - 9 &= 0 \\
 4x^2 - 16x - 9 + 9 &= 0 + 9 \\
 \frac{4x^2 - 16x}{4} &= \frac{9}{4} \\
 x^2 - 4x + (-2)^2 &= \frac{9}{4} - (-2)^2 \\
 (x - 4)^2 &= \frac{9}{4} + \frac{4 \times 4}{1 \times 4} \\
 (x - 4)^2 &= \frac{9}{4} + \frac{16}{4} \\
 (x - 4)^2 &= \frac{25}{4} \\
 \sqrt{(x - 4)^2} &= \sqrt{\frac{25}{4}} \\
 x - 4 + 4 &= 4 \pm \frac{5}{2} \\
 \therefore x = \frac{9}{2} \quad \text{or} \quad -\frac{1}{2}
 \end{aligned}$$

Task 4:

$$\begin{aligned}
 d &= (1+3) \times (0+9) \times (2+0+0+1) \\
 d &= (4) \times (9) \times (3) \\
 d &= 108 \text{ cm}^2
 \end{aligned}$$

FACTORISE

$$\begin{aligned}
 108 &= (2x - 7) \times 3x + (3x + 4) \times (x) \\
 &= 6x^2 - 21x + 3x^2 + 4x \\
 \frac{108}{9} &= \frac{9x^2}{9} - \frac{17x}{9} \\
 \frac{12}{1} + \left(\frac{17}{9x2}\right)^2 &= x^2 - \frac{17}{9}x + \left(\frac{1}{9x2}\right)^2 \\
 \frac{12}{1} \times 9 + \left(\frac{17}{9x2}\right)^2 \times 9 &= x^2 \times 9 - \frac{17}{9}x \times 9 + \left(\frac{17}{9x2}\right)^2 \times 9 \\
 108 + \frac{1156}{9}x^2 &= \frac{1237}{9}x^2 - 17x \\
 108 + \frac{1156}{9}x^2 - \left(\frac{1237}{9}x^2 - 17\right) &= \frac{1237}{9}x^2 - 17x - \left(\frac{1237}{9}x^2 - 17\right) \\
 108 - 9x^2 + 17x &= 0
 \end{aligned}$$