

$$I_2 = \sum_{r=1}^{n} \frac{r^4}{n^5}$$

$$\frac{1}{n^5} I_2 = \lim_{n \rightarrow \infty} \frac{1}{n} \sum_{r=1}^{n} \left(\frac{r}{n}\right)^4 = \int_0^1 x^4 dx = \frac{1}{5}$$

$$I_1 + I_2$$

$$\frac{1}{4} - \frac{1}{5} = \frac{1}{20}$$

$$Q2 \quad \lim_{n \rightarrow \infty} \left[\frac{n+1}{n^2+1^2} + \frac{n+2}{n^2+2^2} + \frac{n+3}{n^2+3^2} + \dots + \frac{3}{5n^2} \right]$$

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$$I_1 = \frac{2n}{5n^2} = \frac{1}{n}$$

$$I_2 = \frac{3n}{5n^2} = \frac{3}{5n}$$

$\therefore$

$$\lim_{n \rightarrow \infty} \sum_{r=1}^{2n} \frac{1}{n} \left(\frac{1 + \frac{r}{n}}{1 + \left(\frac{r}{n}\right)^2} \right)$$

$$\therefore I = \int_0^2 \frac{1+x}{1+x^2} dx$$

$$\lim_{n \rightarrow \infty} \left(\frac{r}{n}\right) = x$$