

11. Mark each as true or false. If the statement is false, correct the statement so that it is true.

16 points

- a. The columns of an 3×8 matrix are linearly independent.

dependent.
more vectors than entries = L.D.
False

- b. Asking whether linear system corresponding to the augmented matrix $[a_1 \ a_2 \ a_3 \ b]$ has a solution amounts to asking whether b is in $\text{Span}\{a_1 \ a_2 \ a_3\}$.

True

- c. If A is a 5×3 matrix and T is a linear transformation defined by $T(x) = Ax$, then the domain of T is $\mathbb{R}^5$.

$$\mathbb{R}^n \rightarrow \mathbb{R}^m$$

$$\mathbb{R}^3 \rightarrow \mathbb{R}^5$$

False the domain is $\mathbb{R}^3$
and the codomain is $\mathbb{R}^5$.

- d. The set $\text{Span}\{u, v\}$ is always visualized as a plane through the origin for any vectors u and v , where vectors u and v are in $\mathbb{R}^3$, and $\vec{u}$ and $\vec{v}$ are scalar multiples of each other.

False

- e. If A is a 4×4 matrix, then the transformation $x \mapsto Ax$ maps $\mathbb{R}^4$ onto $\mathbb{R}^4$.

False.

if there are four pivots,
one in each row.

- f. If x and y are linearly independent, and if $\{x, y, z\}$ is linearly dependent, then z is in the $\text{Span}\{x, y\}$.

True.

- g. Every linear transformation is a matrix transformation.

False. Derivatives are LT.

Every matrix transformation is a linear transformation.

- h. A linear transformation $T: \mathbb{R}^n \rightarrow \mathbb{R}^m$ always maps the origin of $\mathbb{R}^n$ to the origin of $\mathbb{R}^m$.

True.