

29. if $a + ib = 0$ where $i = \sqrt{-1}$, then $a = b = 0$
30. if $a + ib = x + iy$, where $i = \sqrt{-1}$, then $a = x$ and $b = y$
31. The roots of the quadratic equation $ax^2 + bx + c = 0$; $a \neq 0$ are $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

The solution set of the equation is $\left\{ \frac{-b + \sqrt{\Delta}}{2a}, \frac{-b - \sqrt{\Delta}}{2a} \right\}$

where $\Delta = \text{discriminant} = b^2 - 4ac$

32. The roots are real and distinct if $\Delta > 0$.
33. The roots are real and coincident if $\Delta = 0$.
34. The roots are non-real if $\Delta < 0$.
35. If α and β are the roots of the equation $ax^2 + bx + c = 0$, $a \neq 0$ then
- $\alpha + \beta = \frac{-b}{a} = -\frac{\text{coeff. of } x}{\text{coeff. of } x^2}$
 - $\alpha \cdot \beta = \frac{c}{a} = \frac{\text{constant term}}{\text{coeff. of } x^2}$
36. The quadratic equation whose roots are α and β is $(x - \alpha)(x - \beta) = 0$
i.e. $x^2 - (\alpha + \beta)x + \alpha\beta = 0$
i.e. $x^2 - Sx + P = 0$ where $S = \text{Sum of the roots}$ and $P = \text{Product of the roots}$.
37. For an arithmetic progression (A.P.) whose first term is (a) and the common difference is (d) .
- $n^{\text{th}} \text{ term} = t_n = a + (n - 1)d$
 - The sum of the first (n) terms $= S_n = \frac{n}{2}(a + l) = \frac{n}{2}\{2a + (n - 1)d\}$
where $l = \text{last term} = a + (n - 1)d$.
38. For a geometric progression (G.P.) whose first term is (a) and common ratio is (γ) ,
- $n^{\text{th}} \text{ term} = t_n = a\gamma^{n-1}$.
 - The sum of the first (n) terms:

$$\begin{aligned} S_n &= \frac{a(1 - \gamma^n)}{1 - \gamma} && \text{if } \gamma < 1 \\ &= \frac{a(\gamma^n - 1)}{\gamma - 1} && \text{if } \gamma > 1 \\ &= na && \text{if } \gamma = 1 \end{aligned}$$

39. For any sequence $\{t_n\}$, $S_n - S_{n-1} = t_n$ where $S_n = \text{Sum of the first } (n) \text{ terms}$.
40. $\sum_{\gamma=1}^n \gamma = 1 + 2 + 3 + \dots + n = \frac{n}{2}(n + 1)$.
41. $\sum_{\gamma=1}^n \gamma^2 = 1^2 + 2^2 + 3^2 + \dots + n^2 = \frac{n}{6}(n + 1)(2n + 1)$.