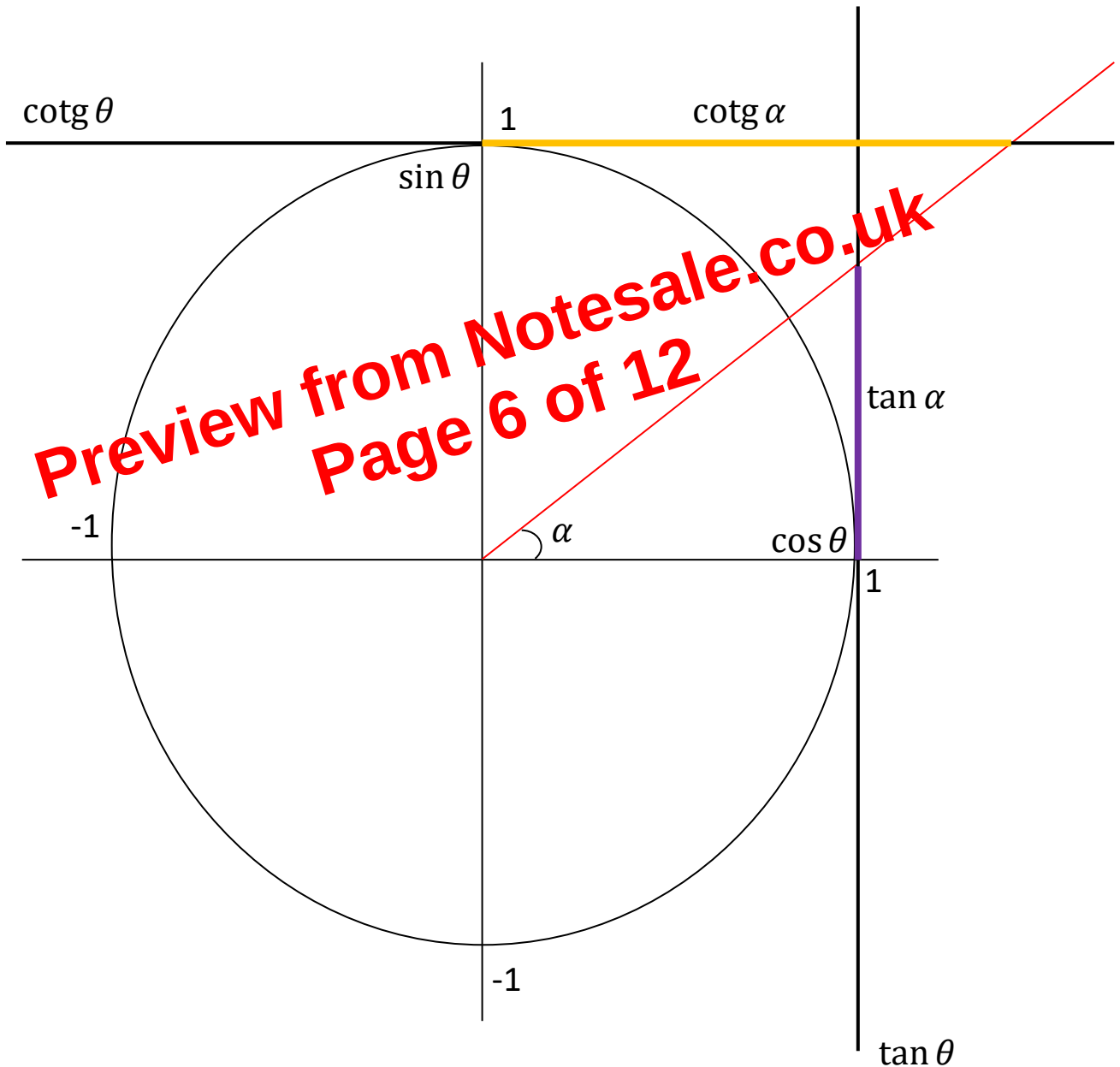


3. Prove that: $\sin 115^\circ \cdot \tan 25^\circ = \cos 65^\circ$.
4. Looking at the circle, try to figure out the values for:
 $\sin 30^\circ$, $\sin 45^\circ$, $\sin 60^\circ$, $\sin 90^\circ$, $\sin 180^\circ$ and so on for $\cos \alpha$.

✓ *Getting deeper into Trigonometric Circle*



5. Expressing $\sin x$, $\cos x$ and $\tan x$ in terms of $\tan \frac{x}{2}$:

$$\sin x = \frac{2 \tan \frac{x}{2}}{1 + \tan^2 \frac{x}{2}}, \quad (18)$$

$$\cos x = \frac{1 - \tan^2 \frac{x}{2}}{1 + \tan^2 \frac{x}{2}}, \quad (19)$$

$$\tan x = \frac{2 \tan \frac{x}{2}}{1 - \tan^2 \frac{x}{2}}. \quad (20)$$

6. Inverse trigonometric functions.

(a) Principal values of inverse trigonometric functions:

$$y = \arcsin x \quad \text{if} \quad x = \sin y \quad \text{and} \quad -\frac{\pi}{2} \leq y \leq \frac{\pi}{2}, \quad (21)$$

$$y = \arccos x \quad \text{if} \quad x = \cos y \quad \text{and} \quad 0 \leq y \leq \pi, \quad (22)$$

$$y = \arctan x \quad \text{if} \quad x = \tan y \quad \text{and} \quad -\frac{\pi}{2} < y < \frac{\pi}{2}, \quad (23)$$

$$y = \operatorname{arccot} x \quad \text{if} \quad x = \cot y \quad \text{and} \quad 0 < y < \pi. \quad (24)$$

(b) Multiple-valued functions:

$$\operatorname{Arc} \sin x = (-1)^n \arcsin x + \pi n, \quad n = 0, \pm 1, \pm 2, \dots, \quad (25)$$

$$\operatorname{Arc} \cos x = \pm \arccos x + 2\pi n, \quad (26)$$

$$\operatorname{Arc} \tan x = \arctan x + \pi n, \quad (27)$$

$$\operatorname{Arc} \cot x = \operatorname{arccot} x + \pi n. \quad (28)$$

Formulas (25) to (28) determine the general expressions for the angles corresponding to given values of trigonometric functions.