Black model for valuation of Interest rate option	Interest rate option: option to enter a FRA in the future. Value of a call option on an (M x N) FRA can be calculated as
	$C_0 = AP \times e^{-r \times (Actutal/365)} \times [FRA_{M \times N} \times N(d_1) - X \times N(d_2)] \times Notional \ principal$
	$AP = accrual\ period = Actual/365$
	Equivalencies: - Long FRA = Long interest rate call + Short interest rate put (exercise rate = current FRA rate)
	- Short FRA = Short interest rate call + Long interest rate put (exercise rate = current FRA rate)
	- Interest rate cap = series of interest rate call with different maturities and same exercise price
	- Interest rate floor = series of interest rate put with different maturities and same exercise price
	- Payer swap = long cap + short floor (exercise rate on cap = exercise rate on floor)
	- Exercise rate on floor = exercise rate on cap = market swap fixed rate → value on cap = value on floor
Black model for valuation of	Swaption: option that gives the holder the right to enter into interest rate swap
Swaption	Payer swaption : fixed-rate payer (receive float)
	Receiver swaption: fixed-rate receiver (pay float)
	Swaption = option on series of CF (annuity) @ each settlement date of the underlying swap that equal to difference between exercise rate on swaption and market swap fixed rate
	$PAY = AP \times PVA \times [SFR \times N(d_1) - X \times N(d_2)] \times Notional\ principal$
	$REC = AP \times PVA \times [X \times N(-d_2) - SFR \times N(-d_1)] \times Notional \ principal$
	In which: PAY = payer swaption
	REC = receiver swaption
	$AP = 1/Number\ of\ settlement\ periodsper\ year\ of\ the\ underlying\ swap$
	SFR = current marke swap fixed rate
	SFR = current marke swap fixed rate $d_1 = \frac{\ln(SFR/X) + (\sigma^2/2) \times T}{\sigma^2 \times \sqrt{T}}$
	$\sigma \times \sqrt{T}$ Equivalencites $\sigma \times \sqrt{T}$
	- Receiver swap = Long receiver swaption + Short payer swaption (same exercise rates)
	- Payer swap = Short receiver swaption + Long payer swaption (same exercise rates)
	- If exercise rate is set so that values of payer swaption = values of receiver swaption → exercise rate - market swap fixed rate
	- Long callable bond = option-free bond + short receiver swaption
	- Long callable bond = option-free bond + short receiver swaption Greeks: sensitivity that capture the relationship between each input and the option price - Inputs: asset price, exercise price, asset price volatility, time to expiration, risk-free rate - Greeks: + Delta: relationship between changes in asset price and changes in option price
Option Greeks	Greeks : sensitivity that capture the relationship between each input and the option price
	- Inputs : asset price, exercise price, asset price volatility, time to expiration, risk-free rate
Option Greeks - Delta	- Greeks :
	+ Delta : relationship between changes in asset price and changes in option price + Gamma : capture the curvature of option value vs. stock price relationship + the option to the curvature of option value vs. stock price relationship + the option to the curvature of option value vs. stock price relationship + the option to the curvature of option value vs. stock price relationship to the option vs.
	+ Vega : measure sensitivity of option price to changes in vol. lifty or recommenderlying asset
	+ Rho : measure the sensitivity of option price to the fire rate
	+ Theta: measure the sensitivity of option like to the lassage of time
	Delta: relationship het were landers, asset price and changes in aption price
Option Greeks - Deita	- Call ratio left a spot tite. Underlying asset — Tall on the decision of the
	Propried to negative - ↑ Underlying as to rice >> Propried ion value
	pelta liculation:
	$Delta_C = e^{-\delta imes T} imes N(d_1) o Out\ of\ the\ money:\ Delta_C\ moves\ closer\ to\ 0\ ; In\ the\ money:\ Delta_C\ moves\ closer\ to\ e^{-\delta imes T}$
	$Delta_P = e^{-\delta \times T} \times N(-d_1) \rightarrow Out \ of \ the \ money: \ Delta_P moves \ closer \ to \ 0; In \ the \ money: \ Delta_P moves \ closer \ to \ -e^{-\delta \times T}$
	Relationship between changes Call / Put option value vs Changes in asset price
	$\Delta C = Delta_C \times \Delta S$ $\Delta P = Delta_P \times \Delta S$
Option Greeks - Gamma	Gamma : Capture the curvation of option value vs. stock price relationship → the rate of change in delta
	Long position in calls and puts : positive gamma
	- Short option → lower gamma
	- Long option → increase gamma
	Gamma is highest for at-the-money options Gamma is low for deep-in-the-money or deep-out-of-money
Option Greeks - Vega	$\Delta C = Delta_C \times \Delta S + \frac{1}{2} \times Gamma \times \Delta S^2$
	$\Delta P = Delta_P \times \Delta S + \frac{1}{2} \times Gamma \times \Delta S^2$
	=
	Vega: measure the sensitivity of the option price to changes in volatility of returns on underlying asset Higher volatility → Increase value f call / put option → positive vega for both call / put
	g, , moreous route roun, postore regular both cull, put
Option Greeks - Rho	Rho : measure the sensitivity of the option price to change in risk-free rate
	(*) Price of European call / put option does not change mch if use different inpts for risk-free rate
Option Greeks - Theta	Theta: sensitivity of option price to passage of time
	Call / Put option approach maturity → decrease spculative vaulue → call / put value decrease (except for deep-in-the-money put options, that might increase value as time passes)
Delta Hedge	Delta-neutral portfolio (delta-neutral hedge): long stock position + short call (or long put) option position > value of portfolio does not change as stock price changes
	number of shares hedged
	Number of snort can needed for detta neage =delta of call option
	Number of long put needed for delta hedge = $\frac{number \text{ of shares hedged}}{number \text{ of shares hedged}}$
	delta of put option
Gamma risk	Gamma risk : risk that stock price might suddenly jump, leaving delta-hedged portfolio unhedged