

similarly, $a_6 = \frac{(-1)^3 a_0}{2^6 \cdot 3! (n+1)(n+2)(n+3)}$

Subs $k=n$ and the values of a_1, a_2, a_3, \dots in equ (2) we get,

$$y = a_0 x^n \left[1 + \frac{(-1)}{2^2 \cdot 1! (n+1)} x^2 + \frac{(-1)^2 x^4}{2^4 \cdot 2! (n+1)(n+2)} + \dots + \frac{(-1)^r x^{2r}}{2^{2r} \cdot r! (n+1)(n+2)\dots(n+r)} \right] \quad (10)$$

Let us put $a_0 = \frac{1}{2^n \Gamma(n+1)}$. Then the solution of

Bessel's equation represented by equ (10) is called Bessel's function of first kind. It is denoted by $J_n(x)$.