



Suppose  $f(x) \geq 0$  the integral  $a \leq x \leq b$

Then the region R under the curve  $y=f(x)$  and between  $x=a$  and  $x=b$  has an area given

$$\text{Area of R} = \int_a^b f(x) dx$$

### Integration by parts

This rule is used to integrate a product of functions.

The product rule differentiation is given as:

$$d(uv)/dx = u dv/dx + v du/dx$$

integrate both sides:

$$uv = \int u dv/dx + \int v du/dx$$

$$\int u dv = uv - \int v du$$

where  $dv$  is the derivative of  $v$  and  $du$  is the derivative of  $u$ .

example:

$$\int x^2 \ln x dx$$

the two factors are  $x^2$  and  $\log x$  thus decide which is  $u$  and  $dv$ .

$$dv = x^2 \quad u = \ln x dx$$

$$v = x^3/3 \quad du = 1/x$$

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