

Algebra

Applications of simultaneous linear equations

1. Vinu bought 5 rulers, 7 ink pads and 3 pens at a cost of Rs. 52. Rosy bought 4 pens, 6 ink pads and 7 rulers for Rs.53 when Paul bought 7 pens and 3 ink pads, the shop keeper took a 50 rupee note from him and paid back the cost of 7 rulers. Find the cost of each.

Solution:

Let the cost of 1 ruler, 1 ink pad and 1 pen be Rs.x, Rs.y, Rs.z respectively.

$$5x + 7y + 3z = 52 \quad \text{-----(1)}$$

$$7x + 6y + 4z = 53 \quad \text{-----(2)}$$

$$3y + 7z = 50 - 7x$$

$$7x + 3y + 7z = 50 \quad \text{-----(3)}$$

$$(1) \times 7 \Rightarrow 35x + 49y + 21z = 364$$

$$(2) \times 5 \Rightarrow 35x + 30y + 20z = 265$$

$$\begin{array}{r} 35x + 49y + 21z = 364 \\ 35x + 30y + 20z = 265 \\ \hline 19y + z = 99 \end{array} \quad \text{-----(4)}$$

$$(2) \Rightarrow 7x + 6y + 4z = 53$$

$$(3) \Rightarrow 7x + 3y + 7z = 50$$

$$\begin{array}{r} 7x + 6y + 4z = 53 \\ 7x + 3y + 7z = 50 \\ \hline 3y - 3z = 3 \\ y - z = 1 \end{array} \quad \text{-----(5)}$$

$$(4) \Rightarrow 19y + z = 99$$

$$(5) \Rightarrow y - z = 1$$

$$\begin{array}{r} 19y + z = 99 \\ y - z = 1 \\ \hline 20y = 100 \end{array}$$

$$y = 5$$

$$\text{From (5)} \quad 5 - z = 1$$

$$z = 4$$

$$\text{From (1)} \quad 5x + 35 + 12 = 52$$

$$5x = 5$$

$$x = 1$$

$$\therefore \text{Cost of 1 ruler} = \text{Rs. 1}$$

$$\text{Cost of 1 ink pad} = \text{Rs. 5}$$