

$$8. \quad \frac{x^2 - y^2}{x^2 + 2xy + y^2} \quad x \quad \frac{xy + y^2}{x^2 - xy}$$

Solution:

$$\begin{aligned} \frac{x^2 - y^2}{x^2 + 2xy + y^2} \quad x \quad \frac{xy + y^2}{x^2 - xy} &= \frac{(x+y)(x-y)}{(x+y)^2} \quad x \quad \frac{y(x+y)}{x(x-y)} \\ &= \frac{y}{x} \end{aligned}$$

$$9. \quad \frac{x^4 - 8x}{2x^2 + 5x - 3} \quad x \quad \frac{2x - 1}{x^2 + 2x + 4} \quad x \quad \frac{x + 3}{x^2 - 2x}$$

$$\text{Solution: } 2x^2 + 5x - 3 = (2x - 1)(x + 3)$$

$$\begin{aligned} \frac{x^4 - 8x}{2x^2 + 5x - 3} \quad x \quad \frac{2x - 1}{x^2 + 2x + 4} \quad x \quad \frac{x + 3}{x^2 - 2x} &= \frac{(x^2 - 4)(x^2 + 2x + 4)}{(2x - 1)(x + 3)} \quad x \quad \frac{2x - 1}{x^2 + 2x + 4} \quad x \quad \frac{x + 3}{x(x - 2)} \\ &= \frac{x}{x} = 1 \end{aligned}$$

$$10. \quad \frac{6x^2 - x - 2}{8x^2 + 6x + 1} \quad x \quad \frac{12x^2 + 7x - 12}{9x^2 + 6x - 8} \quad x \quad \frac{12x^2 - 13x - 4}{12x^2 - 25x + 12}$$

Solution:

$$\begin{aligned} 6x^2 - x - 2 &= 6x^2 - 4x + 3x - 2 \\ &= 2x(3x - 2) + 1(3x - 2) = (3x - 2)(2x + 1) \\ 8x^2 + 6x + 1 &= 8x^2 + 4x + 2x + 1 \\ &= 4x(2x + 1) + 1(2x + 1) = (2x + 1)(4x + 1) \\ 12x^2 - 7x - 12 &= 12x^2 + 16x - 9x - 12 \\ &= 4x(3x + 4) - 3(3x + 4) = (3x + 4)(4x - 3) \\ 9x^2 + 6x - 8 &= 9x^2 + 12x - 16x - 8 \\ &= 3x(3x + 4) - 2(3x + 4) = (3x + 4)(3x - 2) \\ 12x^2 - 13x - 4 &= 12x^2 - 16x + 3x - 4 \end{aligned}$$