

solution: $\Omega = \int_0^1 \arcsin(x) \arccos(x) dx$

IBP $\sin^{-1}(x) = u \quad \frac{du}{dx} = \frac{1}{\sqrt{1-x^2}} \quad v = \int \cos^{-1}(x) dx =$

$$= x \cdot \cos^{-1}(x) - \sqrt{1-x^2}$$

$$\Omega = [uv]_0^1 - \int_0^1 \frac{x \cdot \cos^{-1}(x)}{\sqrt{1-x^2}} dx + \int_0^1 dx =$$

$$= \left[\frac{\sin^{-1}(x) (x \cdot \cos^{-1}(x) - \sqrt{1-x^2})}{1} \right]_0^1 - \int_0^1 \frac{x \cdot \cos^{-1}(x)}{\sqrt{1-x^2}} dx +$$

$$- \int_0^1 dx = 1 - \int_0^1 \frac{x \cdot \cos^{-1}(x)}{\sqrt{1-x^2}} dx \quad \cos^{-1}(x) = t \quad \frac{dt}{dx} = \frac{-1}{\sqrt{1-x^2}}$$

$$\Omega = 1 - \int_0^{\frac{\pi}{2}} \frac{t \cdot \cos(t)}{\sqrt{1-x^2}} \times \sqrt{1-x^2} dt = 1 - \int_0^{\frac{\pi}{2}} t \cdot \cos(t) dt =$$

IBP $\times \angle$

$$= 1 - [t \cdot \sin(t)]_0^{\frac{\pi}{2}} + \int_0^{\frac{\pi}{2}} \sin(t) dt = 1 - \frac{\pi}{2} - \left|_0^{\frac{\pi}{2}} \cos(t) \right| =$$

$$= 1 - \frac{\pi}{2} - (0 - 1) = 2 - \frac{\pi}{2}$$

answer: $\int_0^1 \sin^{-1}(x) \cos^{-1}(x) dx = 2 - \frac{\pi}{2}$