

increases (decreases); (ii) they are inversely proportional, i.e. when one increases (decreases) the other decreases (increases); (iii) no relation. These three situations can be stated as follows statistically (i) positively correlated (ii) negatively correlated (iii) no-correlation.

### SCATTER DIAGRAM

It is the simplest way of the diagrammatic representation of bivariate data. Let  $X$  and  $Y$  be the two variables under study with  $n$  observation each. If we plot  $(X_1, Y_1), (X_2, Y_2), \dots, (X_n, Y_n)$  on a graph sheet, the resulting diagram gives us a vague idea about the correlation between these two variables  $X$  and  $Y$ .

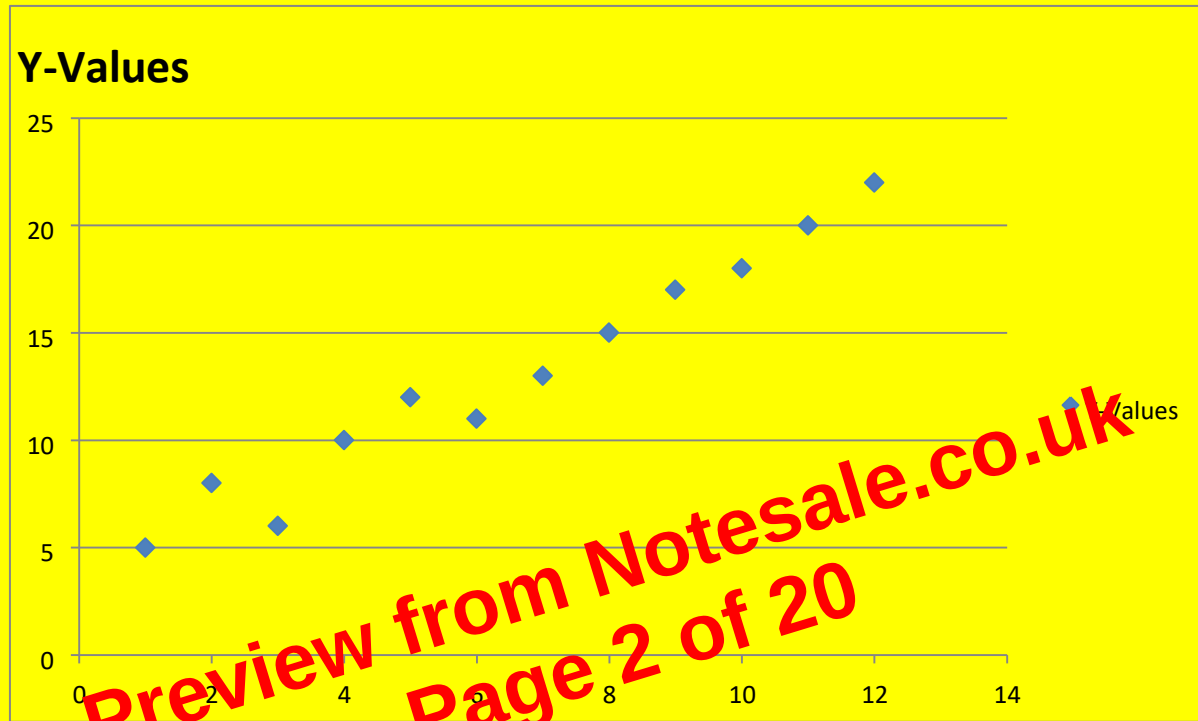


Figure 1

Fig 1 represents that there is a positive correlation between the variables  $X$  and  $Y$ .

S.D                                      2                                      4

$$r = 0.8$$

Find the two regression equations

### Solution

Regression equation  $Y$  on  $X$

$$b_{yx} = r \cdot \frac{\sigma_y}{\sigma_x} = 0.8 \times \frac{2}{4} = 0.4$$

$$(Y - \bar{Y}) = b_{yx} (X - \bar{X})$$

$$(Y - 10) = 0.4(X - 15)$$

$$Y - 10 = 0.4X + 10 - 6$$

$$Y = 0.4X + 10 - 6$$

$$Y = 0.4X + 4$$

Regression equation  $X$  on  $Y$

$$b_{xy} = r \cdot \frac{\sigma_x}{\sigma_y} = 0.8 \times \frac{4}{2} = 1.6$$

$$(X - \bar{X}) = b_{xy} (Y - \bar{Y})$$

$$(X - 15) = 1.6(Y - 10)$$

$$X = 1.6Y - 16 + 15$$

$$X = 1.6Y - 1$$

### Example

Find the regression equation for the following

|       |    |    |    |    |
|-------|----|----|----|----|
| $X$ : | 2  | 4  | 6  | 8  |
| $Y$ : | 10 | 20 | 25 | 30 |

### Solution

Regression equation

|     |     |               |       |         |         |          |
|-----|-----|---------------|-------|---------|---------|----------|
| $X$ | $Y$ | $d_x = X - 5$ | $d_y$ | $d_x^2$ | $d_y^2$ | $d_{xy}$ |
|-----|-----|---------------|-------|---------|---------|----------|

11. Calculate the regression equation for the following data and also compute Karl Pearson's coefficient of correlation:

|                          |     |     |     |     |     |     |
|--------------------------|-----|-----|-----|-----|-----|-----|
| No. of students ( $X$ ): | 800 | 600 | 900 | 700 | 500 | 400 |
| No. of Passed ( $Y$ ):   | 480 | 300 | 450 | 560 | 450 | 310 |

12. To study the effect of rain on yield of wheat the following results were obtained.

|                  |      |     |
|------------------|------|-----|
|                  | Mean | S.D |
| Yield( $X$ ):    | 800  | 12  |
| Rainfall( $Y$ ): | 50   | 2   |

$$r = +0.80$$

Estimate the yield when the rainfall is 80 inches.

13. Find the two regression equations, regression co-efficient of correlation from the following figures.

$$\sum X = 120, \quad \sum Y = 432, \quad \sum XY = 4992, \quad \sum X^2 = 1394, \quad \sum Y^2 = 18,252, \quad \text{and } n = 12$$

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