You must calculate the complexity of algorithm

1: sum = 02: **for** *i* = 1 to 4*n* **do** 3: for i = 1 to $4n^2$ with step 4 do 4: for k = n to 1 with step -2 do sum = sum + 15: 6: end for 7: end for 8: end for

Solution:

$$\sum_{i=1}^{4n} \sum_{j=1}^{n^2} \sum_{k=1}^{\frac{n}{2}} O(1) = O(1) \cdot \sum_{i=1}^{4n} \sum_{j=1}^{n^2} \sum_{k=1}^{\frac{n}{2}} 1 = O(1) \cdot \sum_{i=1}^{4n} \sum_{j=1}^{n^2} \frac{n}{2} = O(1) \cdot \frac{n}{2} \cdot \sum_{i=1}^{4n} \sum_{j=1}^{n^2} 1 = O(1) \cdot \frac{n}{2} \cdot \sum_{i=1}^{4n} \sum_{j=1}^{2n} \frac{n}{2} \cdot \sum_{i=1}^{4n} \sum_{j=1}^{2n} \frac{n}{2} \cdot \sum_{i=1}^{4n} \sum_{j=1}^{2n} \frac{n}{2} \cdot \sum_{i=1}^{4n} \sum_{j=1}^{4n} \sum_{j=1}^{2n} \frac{n}{2} \cdot \sum_{i=1}^{4n} \sum_{j=1}^{4n} \sum_{j=1}^{4n} \sum_{i=1}^{4n} \sum_{j=1}^{4n} \sum_{j=$$

$$O(1) \cdot \frac{n}{2} \cdot \sum_{i=1}^{4n} n^2 = O(1) \cdot \frac{n}{2} \cdot n^2 \cdot \sum_{i=1}^{4n} 1 = O(1) \cdot \frac{n}{2} \cdot n^2 \cdot 4n = O(1) \cdot 2n^4$$

The complexity of algorithm is O(n⁴). We do not care about constant O(1)*2 Explanation: • Generally, we put the constants (0, 1, 2, O(1), ...) out of the sum. In this point of the sum.

this example O(1) is constant. Moreover, when we have this sum $\sum_{i=1}^{n} n$, we can do $n * \sum_{i=1}^{n} 1$

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$$\sum_{i=1}^{n} 1 = (n-1)+1$$