

You must calculate the complexity of algorithm

```
1: sum = 0
2: for i = 1 to 4n do
3:     for j = 1 to 4n2 with step 4 do
4:         for k = n to 1 with step -2 do
5:             sum = sum + 1
6:         end for
7:     end for
8: end for
```

Solution:

$$\sum_{i=1}^{4n} \sum_{j=1}^{n^2} \sum_{k=1}^{\frac{n}{2}} O(1) = O(1) \cdot \sum_{i=1}^{4n} \sum_{j=1}^{n^2} \sum_{k=1}^{\frac{n}{2}} 1 = O(1) \cdot \sum_{i=1}^{4n} \sum_{j=1}^{n^2} \frac{n}{2} = O(1) \cdot \frac{n}{2} \cdot \sum_{i=1}^{4n} \sum_{j=1}^{n^2} 1 =$$
$$O(1) \cdot \frac{n}{2} \cdot \sum_{i=1}^{4n} n^2 = O(1) \cdot \frac{n}{2} \cdot n^2 \cdot \sum_{i=1}^{4n} 1 = O(1) \cdot \frac{n}{2} \cdot n^2 \cdot 4n = O(1) \cdot 2n^4$$

The complexity of algorithm is $O(n^4)$. We do not care about constant $O(1) \cdot 2$

Explanation:

- Generally, we put the constants (0, 1, 2, $O(1)$, ...) out of the sum. In this example $O(1)$ is constant. Moreover, when we have this sum $\sum_{i=1}^n n$, we can do $n * \sum_{i=1}^n 1$
- $\sum_{i=1}^n 1 = (n-1)+1$