

16. Find the derivative of $y = e^x$

17. Evaluate the definite integral of $x^3 dx$ from $x=1$ to $x=2$

18. Find the equation of the tangent line to the graph of $y = \ln(x)$ at the point $(1,0)$

19. Evaluate the definite integral of $(1/x^3) dx$ from $x=1$ to $x=2$

20. Find the equation of the normal line to the graph of $y = \sin(x)$ at the point $(\pi/4, 1/\sqrt{2})$

Answer:

1. Evaluate the limit as x approaches 0 of $(\sin(x))/x$:

Using L'Hopital's rule, we can take the limit of the derivative of numerator and denominator. The derivative of $\sin(x)$ is $\cos(x)$ and the derivative of x is 1. So the limit becomes:

$$\lim_{x \rightarrow 0} (\sin(x))/x = \lim_{x \rightarrow 0} (\cos(x))/1 = \cos(0) = 1$$

2. Find the derivative of $y = x^2$:

The derivative of $y = x^2$ is $dy/dx = 2x$

3. Evaluate the definite integral of x^2 from $x=0$ to $x=1$:

The antiderivative of x^2 is $(x^3)/3$. So the definite integral is:

$$(x^3)/3 \text{ from } 0 \text{ to } 1 = (1^3)/3 - (0^3)/3 = (1/3) - 0 = 1/3$$

4. Find the second derivative of $y = \cos(x)$: