

# TRIGONOMETRIC FUNCTIONS

$$③ \tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$$

$$④ \cot(A \pm B) = \frac{\cot B \mp \cot A}{\cot A \cot B \mp 1}$$

$$\bullet \sin^2 A - \sin^2 B = \cos^2 B - \cos^2 A = \sin(A+B) \sin(A-B)$$

$$\bullet \cos^2 A - \sin^2 B = \cos^2 B - \sin^2 A = \cos(A+B) \cos(A-B)$$

## II) Degree and Radian

- $\sin^2 \theta + \cos^2 \theta = 1$
- $1 + \tan^2 \theta = \sec^2 \theta$
- $1 + \cot^2 \theta = \operatorname{cosec}^2 \theta$

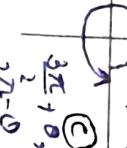
$$\boxed{\pi^c = 180^\circ}$$

Radian Measure =  $\frac{\pi}{180} \times \text{Degree Measure}$

Degree Measure =  $\frac{180}{\pi} \times \text{Radian Measure}$

$\boxed{R = \pi \theta}$  Note:-  $\theta$  is in Radian

## III) Quadrant System

- |   |   |                                      |
|---|---|--------------------------------------|
| ⑤ $r_{12+0}, r_{12-\theta}, \alpha, \frac{\pi}{2\pi+\theta}$<br> | ⑥ $r_{12-0}, r_{12-\theta}, \alpha, \frac{\pi}{2\pi-\theta}$<br> | ⑦: Tan and cot<br><br>⑧: Cos and sec |
|---|---|--------------------------------------|

## IV) Value of Any Angle

①  $\frac{\pi}{2} \times \text{odd multiple} \Rightarrow \sin \rightarrow \cos, \tan \rightarrow \cot, \csc \rightarrow \sec$

②  $\times \text{even multiple} \Rightarrow \tan \rightarrow \tan, \cot \rightarrow \cot, \sec \rightarrow \sec$

③ Check the quadrant for the sign as per the original function

Sin and cos ki kahaani

**Sin** ☺ Friendly, Loyal, Accomodating

**Cos** ☹ Stubborn, Angry, Non-Accomodating

①  $\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$

②  $\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$

## VII) Double Angle Formulae

① $\sin 2A = 2 \sin A \cos A$ ② $\cos 2A = \cos^2 A - \sin^2 A$ ③ $\tan 2A = \frac{2 \tan A}{1 + \tan^2 A}$	④ $\sin 3A = 3 \sin A - 4 \sin^3 A$ ⑤ $\cos 3A = 4 \cos^3 A - 3 \cos A$	⑥ $\tan 3A = \frac{3 \tan A - \tan^3 A}{1 - 3 \tan^2 A}$
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## VIII) Triple Angle Formulae

$$\sin C + \sin D = 2 \sin \left( \frac{C+D}{2} \right) \cos \left( \frac{C-D}{2} \right)$$

$$② \sin C - \sin D = 2 \cos \left( \frac{C+D}{2} \right) \sin \left( \frac{C-D}{2} \right)$$

$$③ \cos C + \cos D = 2 \cos \left( \frac{C+D}{2} \right) \cos \left( \frac{C-D}{2} \right)$$

$$④ \cos C - \cos D = -2 \sin \left( \frac{C+D}{2} \right) \sin \left( \frac{C-D}{2} \right)$$

## IX) Naam Kya Di?

$$① 2 \sin A \cos B = \sin(A+B) + \sin(A-B)$$

$$② 2 \cos A \sin B = \sin(A+B) - \sin(A-B)$$

$$③ 2 \cos A \cos B = \cos(A+B) + \cos(A-B)$$

$$④ -2 \sin A \sin B = \cos(A+B) - \cos(A-B)$$

$$⑤ \sin \theta \cdot \sin(\theta - \epsilon)$$

$$⑥ \sin(\theta + \epsilon) \cdot \frac{1}{4} \sin 3\theta$$

## Imp Result

$$1 \cdot \sin(A+B) \cdot \sin(A-B)$$

$$= \sin^2 A - \sin^2 B$$

$$= \cos^2 B - \cos^2 A$$

$$2 \cdot \cos(A+B) \cdot \cos(A-B)$$

$$= \cos^2 A - \sin^2 A$$

$$= \cos^2 B - \sin^2 B$$