

Therefore, the manufacturer should produce 320 units of A and 300 units of B to maximize the number of units produced subject to the constraints.

13. Find the inverse of the matrix $A = \begin{bmatrix} 3 & 2 \\ 1 & 4 \end{bmatrix}$:

The inverse of a 2×2 matrix $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ is given by $(1/\det(A)) * \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$, where $\det(A)$ is the determinant of A.

So, for $A = \begin{bmatrix} 3 & 2 \\ 1 & 4 \end{bmatrix}$, we have $\det(A) = (34) - (21) = 10$.

Therefore, the inverse of A is $(1/10) * \begin{bmatrix} 4 & -2 \\ -1 & 3 \end{bmatrix}$.

14. If $\sin(x+20) = \cos(x-10)$, find the value of x:

Using the identity $\sin(a+b) = \sin(a)\cos(b) + \cos(a)\sin(b)$, we can rewrite the given equation as $\sin(x)\cos(20) + \cos(x)\sin(20) = \cos(x)\cos(10) + \sin(x)\sin(10)$.

Simplifying this, we get $\tan(x) = (\cos(10) - \cos(20)) / \sin(20) = -0.9619$ (approx).

Using a calculator or trigonometric tables, we find that the angle whose tangent is -0.9619 is approximately -42.3 degrees (or -0.738 radians).

Therefore, $x = -20 - 0.738 = -20.738$ degrees (or -0.362 radians).

15. If the sum of the first n terms of an arithmetic progression is $5n^2 - 3n$, find the 10th term:

The sum of the first n terms of an arithmetic progression is given by the formula $S_n = n/2[2a + (n-1)d]$, where a is the first term and d is the common difference.

From the given information, we have $S_{10} = 5(10)^2 - 3(10) = 470$, and $S_9 = 5(9)^2 - 3(9) = 378$.

Subtracting S_9 from S_{10} , we get the 10th term (which is the difference between the sums of the first 10 terms and the first 9 terms):

$$T_{10} = S_{10} - S_9 = \frac{10}{2}[2a + (10-1)d] - \frac{9}{2}[2a + (9-1)d]$$

Simplifying this, we get $T_{10} = 12 - 6d$.

We still need to find the values of a and d to determine T_{10} . Using the formula for S_9 and S_{10} , we can set up two equations in two variables:

$$S_9 = \frac{9}{2}[2a + (9-1)d] = 5(9)^2 - 3(9)$$

$$S_{10} = \frac{10}{2}[2a + (10-1)d] = 5(10)^2 - 3(10)$$

Simplifying these equations, we get:

$$9a + 36d = 360$$

$$10a + 45d = 515$$

Solving for a and d, we get $a = 5$ and $d = 4$.

Substituting these values into the expression we obtained for T_{10} , we get:

$$T_{10} = 12 - 6(4) = 68.$$

Therefore, the 10th term of the arithmetic progression is 68.

16. Let the side of the square park be "a". Then, its area is $a^2 = 144$ sq. meters, so $a = 12$ meters.

Let the width of the path be "x". Then, the side of the new square formed by the outer edge of the path is $(a + 2x)$ meters. The area of the path is then:

$$\text{Area of path} = (a + 2x)^2 - a^2$$

Since the area of the path is equal to the area of the park, we have:

$$(a + 2x)^2 - a^2 = 144$$

Expanding the left side of the equation, we get:

$$4ax + 4x^2 = 144$$