

10. If x and y are of same sign, then the value of $\frac{x^3}{2} \operatorname{cosec}^2\left(\frac{1}{2} \tan^{-1} \frac{x}{y}\right) + \frac{y^3}{2} \sec^2\left(\frac{1}{2} \tan^{-1} \frac{y}{x}\right)$ is equal to
 (A) $(x-y)(x^2+y^2)$ (B) $(x+y)(x^2-y^2)$ (C) $(x+y)(x^2+y^2)$ (D) $(x-y)(x^2-y^2)$
11. For $f(x) = \tan^{-1} \left(\frac{(\sqrt{12}-2)x^2}{x^4+2x^2+3} \right)$
 (A) $f_{\max} = \frac{\pi}{12}$ (B) $f_{\min} = 0$ (C) f_{\min} does not exist (D) $f_{\max} = \frac{\pi}{2}$
12. If $f(x) = \begin{cases} x+1, & x \leq 0 \\ 2-x, & x > 0 \end{cases}$ and $g(x) = \begin{cases} x^2+1, & x \geq 1 \\ 2x-3, & x < 1 \end{cases}$ then
 (A) Range of $\text{gof}(x)$ is $(-\infty, -1) \cup [2, 5]$ (B) Range of $\text{gof}(x)$ is $(-\infty, -1) \cup [2, 5)$
 (C) $\text{gof}(x)$ is one-one for $x \in [0, 1]$ (D) $\text{gof}(x)$ is many one for $x \in [0, 1]$
13. If $f(x)$ is identity function, $g(x)$ is absolute value function and $h(x)$ is reciprocal function then
 (A) $\text{fogoh}(x) = \text{hogof}(x)$ (B) $\text{hog}(x) = \text{hogof}(x)$
 (C) $\text{gofofohogof}(x) = \text{gohog}(x)$ (D) $\text{hohohoh}(x) = f(x)$
14. The function $y = \frac{x}{1+|x|} : \mathbb{R} \rightarrow \mathbb{R}$ is
 (A) one-one (B) onto (C) odd (D) into
15. If α, β, γ are roots of equation $\tan^{-1}(|x^2+2x| + |x+3| - ||x^2+2x| - |x+3||) + \cot^{-1}\left(-\frac{1}{2}\right) = \pi$ in ascending order ($\alpha < \beta < \gamma$) then
 (A) $\sin^{-1}\gamma$ is defined (B) $\sec^{-1}\alpha$ is defined
 (C) $\gamma - \beta = \sqrt{2}$ (D) $|\beta| > |\gamma|$
16. If $f(x)$ and $g(x)$ are two polynomials such that the polynomial $n(x) = xf(x^3) + x^2g(x^6)$ is divisible by $x^2 + x + 1$, then
 (A) $f(1) = g(1)$ (B) $f(1) = -g(1)$ (C) $h(1) = 0$ (D) all of these
17. $1 + [\sin^{-1}x] > [\cos^{-1}x]$ where $[\cdot]$ denotes GIF, if $x \in$
 (A) $(\cos 1, \sin 1)$ (B) $[\sin 1, 1]$ (C) $(\cos 1, 1)$ (D) $[\cos 1, 1]$
18. If the solution of equation $\sin(\tan^{-1}x) = \frac{1}{\sqrt{4 - [\sin(\cos^{-1}x) + \cos(\sin^{-1}x)]^2}}$ is a , then
 (A) $\sin^{-1}a + \cos^{-1}a = \frac{\pi}{2}$ (B) $2\sin^{-1}a + \cos^{-1}a = \frac{\pi}{2}$ (C) $\sin^{-1}a + 3\cos^{-1}a = \frac{3\pi}{2}$ (D) $\tan^{-1}a + \cos^{-1}a = \frac{\pi}{2}$
19. If $f(x) = \frac{2^{\{x\}} - 1}{2^{\{x\}} + 1}$ then (where $\{x\}$ represent fractional part of x)
 (A) $D_f \in \mathbb{R}$ (B) $R_f \in [0, \frac{1}{3})$ (C) period of $f(x)$ is 1 (D) $f(x)$ is even function
20. Which of the following is true for $f(x) = (\cos x)^{\cos x}$, $x \in \left[-\cos^{-1}\frac{1}{e}, \cos^{-1}\frac{1}{e}\right]$
 (A) $R_f \in \left[\left(\frac{1}{e}\right)^{1/e}, 1\right]$ (B) $f(x)$ is increasing (C) $f(x)$ is many-one (D) $f(x)$ is maximum at $x = 0$
21. If $f(x) = \tan^{-1}\left(\frac{2x}{1-x^2}\right)$ is a bijective function from set A to set B then which of the following may be true
 (A) $A = (-\infty, -1)$, $B = \left(0, \frac{\pi}{2}\right)$ (B) $A = (-1, 1)$, $B = \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$
 (C) $A = [1, \infty)$, $B = \left(-\frac{\pi}{2}, 0\right]$ (D) All of these