

FIRST MODEL:

Galor-Zeira (1993) : The credit market imperfection approach

Production of the final good:

Y_t = Y^A + Y^M

Production of final good = production agricultural + production manufacturing

Production in the agricultural sector = amount of labour * wage of unskilled worker

Production in the Agricultural sector:

Y^A = F^A(L_t) = w^u L_t

L_t - the number of unskilled workers producing in the agricultural sector

Production in manufacturing is a function of human and physical capital Basically takes wage a constant and given

Production in the Manufacturing sector:

Y^M = F^M(H_t, K_t)

H_t - the number of skilled workers producing in the manufacturing sector

K_t - the stock of capital

F^M is a classical CRS production function

L_t + H_t = 1

Individuals:

Over-lapping generation model

A generation of size 1 is born every period and lives for two periods

Each individual has one parent and one child

A young person and an adult form a dynasty

In every period there's two types of individuals

In their first life period:

Individuals are endowed with a parental bequest & invest in human and/or physical capital

The young don't work but receive help from their parents

Young make decision in how much to invest in education in t+1

In their second life period:

Individuals supply labour inelastically, consume and bequeath

Adults make a decision: to allocate to consumption or transfer to offspring

u = utility of individual i who is young and born in period t

log c(t+1) = obtains utility from consumption in the future

log b(t+1) = obtains utility from requesting to next generation

Preferences of individual i born in t are defined by the utility function:

u_i^t = (1 - \beta) log c_{t+1}^i + \beta log b_{t+1}^i

where \beta \in (0, 1).

Budget constraint

c_{t+1} + b_{t+1}^i = I_{t+1}^i

→

b_{t+1}^i = b(I_{t+1}^i) = \beta I_{t+1}^i

Budget constraint: consumption next period + bequest next period

Bequest next period is a function and a fraction of income

The production of human capital

there is an indivisible cost, h, invested in t

(in the first period of life) to become skilled

in t + 1

To become skilled, there is a fixed cost, h.

Capital Markets and Prices: ignore, except

We assume that:

R = 1 + r : is a given, constant and exogenous

Ws = Wu : wages are constant over time, and low skill wage = high skill wage

Capital markets and prices

unrestricted international capital flows at the world interest rate r.

→ k_t = k for all t such that:

f'(k) + 1 - \delta = 1 + r = R

→

w_t^s = w^s = f(k) - f'(k)k

The unskilled wage is

w_t^u = w^u

A model of credit constraints:

parent's income is used as collateral

markets are not perfect

borrowing rate > lending rate

theta * R > 1 = rate you borrow at

hR = the return on capital

hR = alternative return on investment (lending the money out)

Ws - Wu = return on investment by becoming skilled

R (interest rate) is small such that it is worth getting education Ws - Wu rather than lending (hR)

Assumption 1: R is sufficiently small such that the gain from investing in education is greater than the alternative return on capital

Assumption 2: theta (the borrowing rate) is sufficiently large such that the inequality reverses.

A1: R is sufficiently small such that

w^s - w^u > hR

the interest rate for borrowers for sake of investment in human capital is

\theta R

where \theta > 1.

A2: \theta is sufficiently large such that:

w^s - w^u < h\theta R

If you don't have money, don't borrow, because the amount you have to pay back (h * theta * R) is higher than the increase in wage:

h * theta * R > Ws - Wu

This mechanism generates the poverty trap

Borrowing 100% (full loan) not a good idea, but what about 90%, 80%...?

Implication: There is a threshold level at which it is worth borrowing the rest (0 < x < 100)

Investment decisions and income

if b_t^i \ge h

I_{t+1}^i = w^s + (b_t^i - h)R

if b_t^i < h

I_{t+1}^i = \max\{w^s - (h - b_t^i)\theta R, w^u + b_t^i R\}

So we need to find which of the two (above) is higher, giving you a threshold where an individual will invest in human capital if and only if b > b^A

where b^A = (Wu - Ws + h * theta * R) / [R * (theta - 1)]

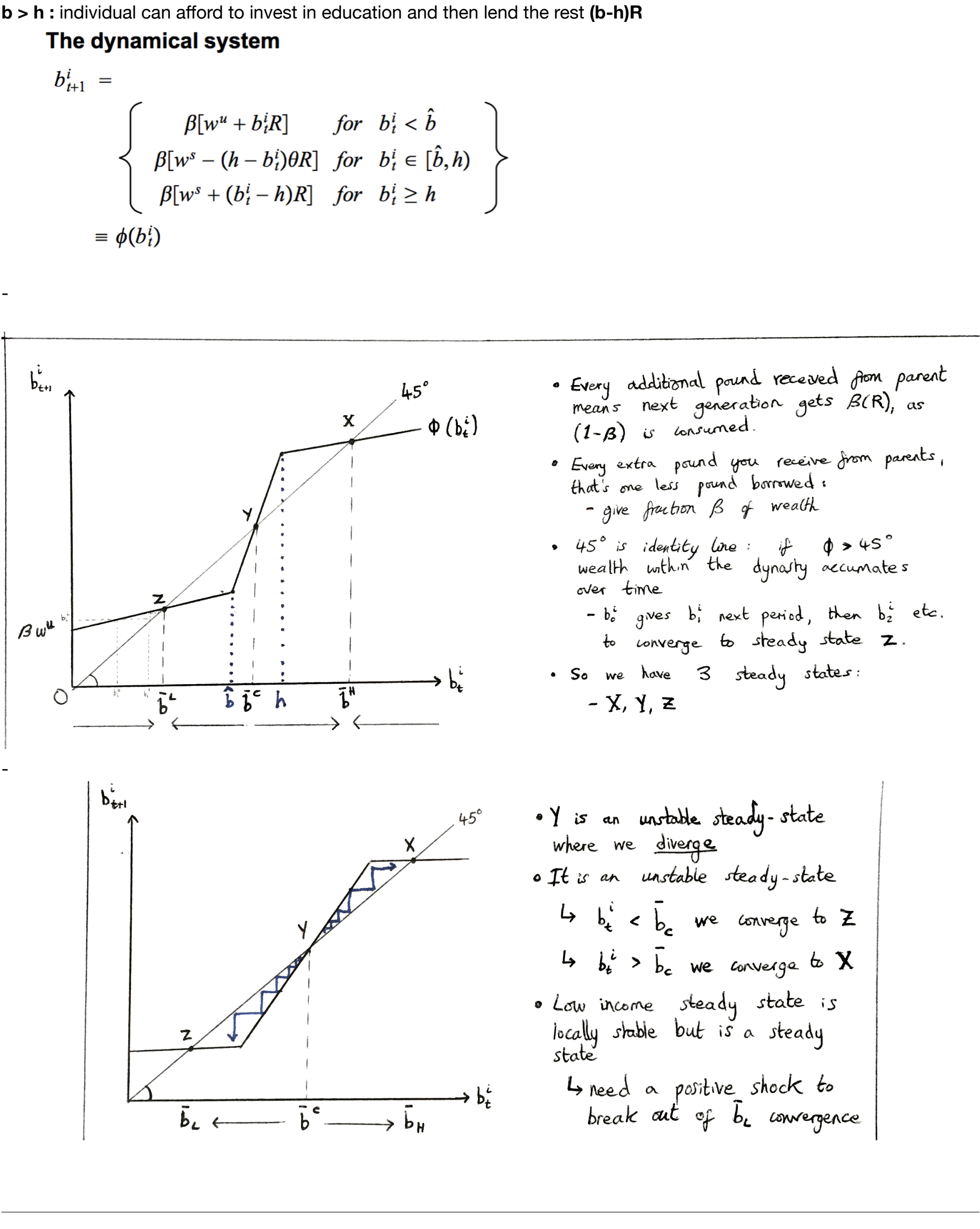
where, as follows from A1 and A2 there exists

\hat{b} = \frac{w^u - w^s + h\theta R}{R(\theta - 1)} \in (0, h)

such that

w^s - (h - \hat{b})\theta R = w^u + \hat{b}R

and individuals choose to invest in human capital if and only if b_t^i \ge \hat{b}.



alternative presentation: the cost of education, which is strictly decreasing in b_t^i

for b_t^i < h, is equal to the return,

(h - \hat{b})\theta R + \hat{b}R

= h\theta R - \hat{b}(\theta - 1)R

= w^s - w^u

The dynamical system: governs the evolution of bequests over time of a dynasty.

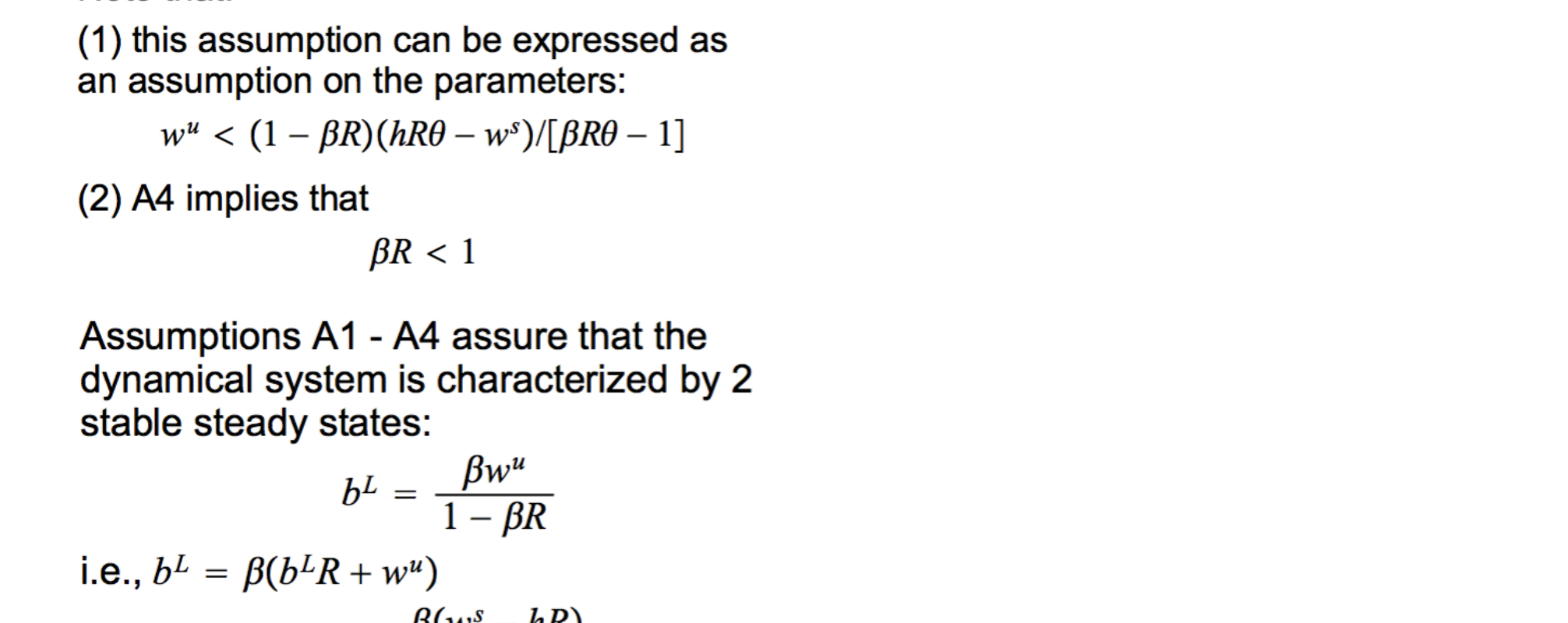
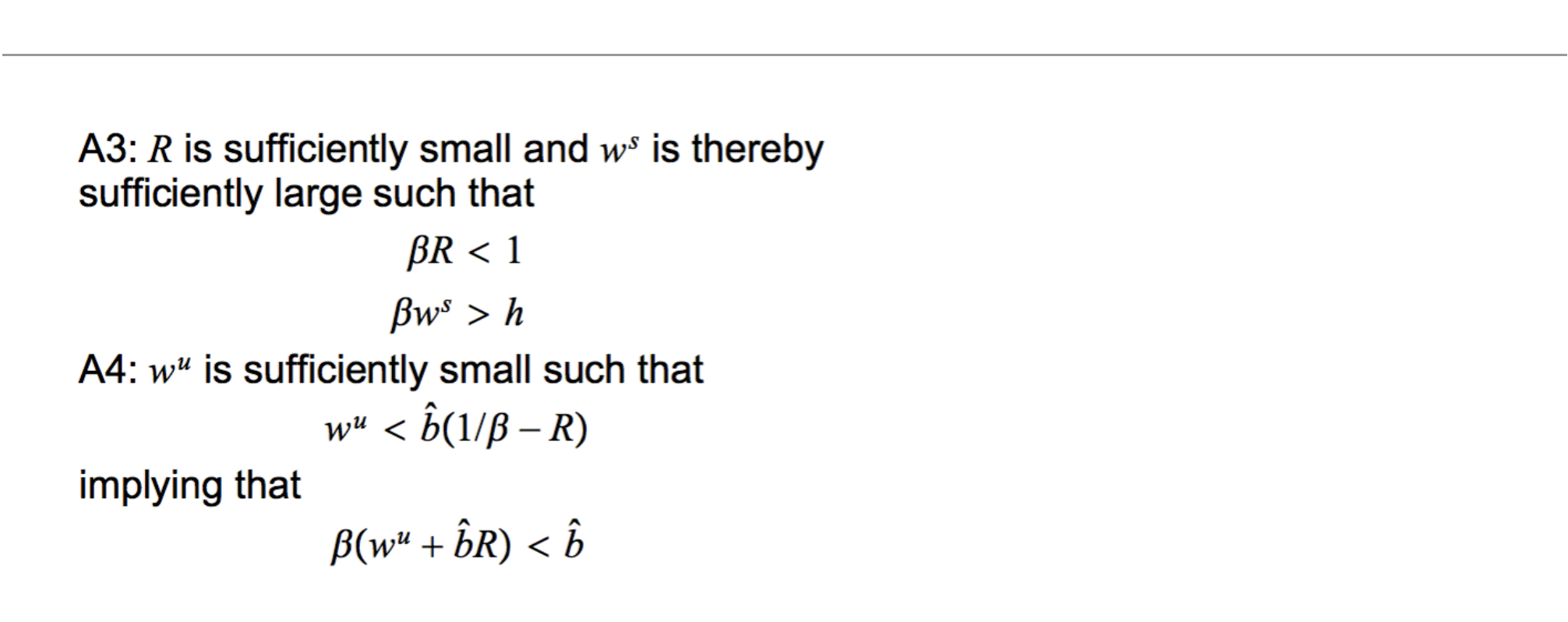
b < b^A : dynasty i individual who receives amount not sufficient to justify borrowing the rest of the cost of education

b for range b^A-h : individual would invest but would have to borrow

b > h : individual can afford to invest in education and then lend the rest (b-h)R

The dynamical system

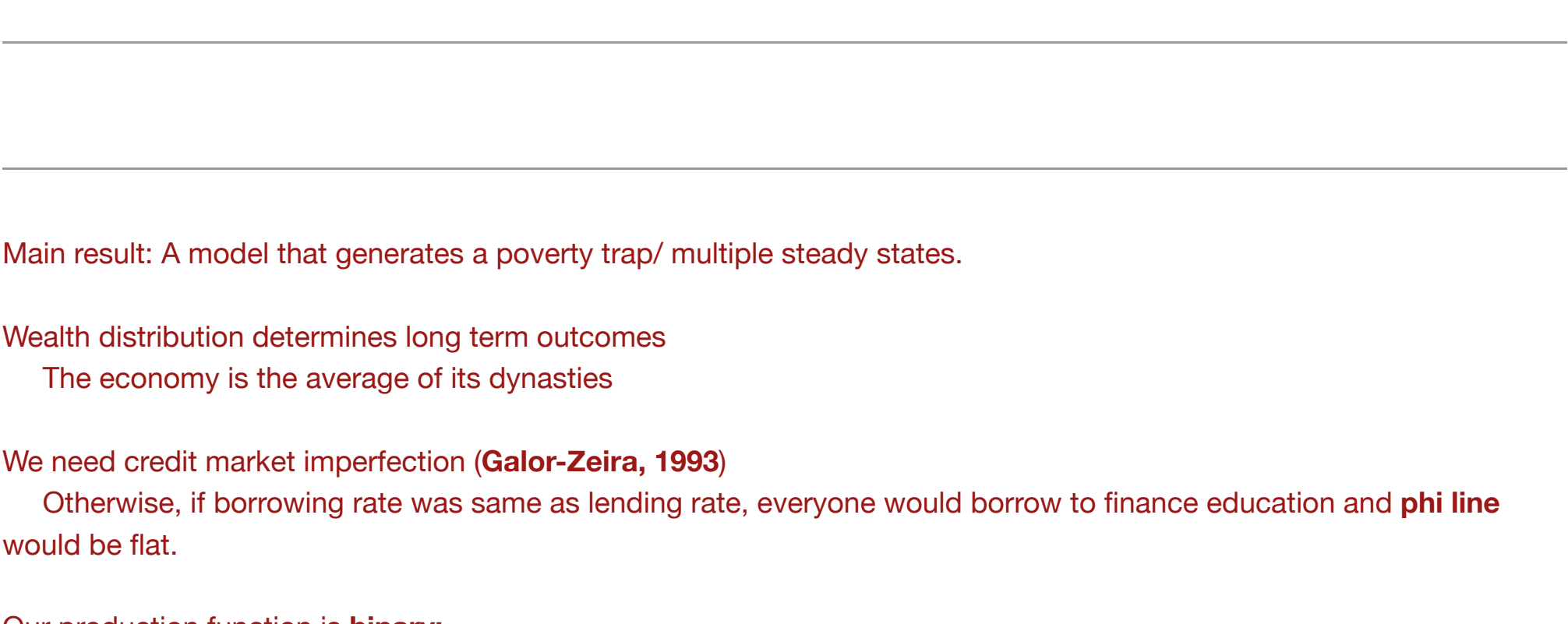
b_{t+1}^i = \begin{cases} \beta[w^u + b_t^i R] & \text{for } b_t^i < \hat{b} \\ \beta[w^s - (h - b_t^i)\theta R] & \text{for } b_t^i \in [\hat{b}, h) \\ \beta[w^s + (b_t^i - h)R] & \text{for } b_t^i \geq h \end{cases} \equiv \phi(b_t^i)



The mechanism

*The need to invest in education to escape poverty trap

Credit market imperfection is that there is a gap in interest rates between borrowers and lenders (risk premium)



If someone gets b^A they will transfer to the next generation less than b^A

This is because N is below the 45 degree line:

So wealth over time in the dynasty is shrinking

\beta(w^u + \hat{b}R) < \hat{b}

which can be rearranged to->

w^u is sufficiently small such that

w^u < \hat{b}(1/\beta - R)

If wage is low then dynasties will be stuck in poverty

Income only increases when:

\beta w^s > h

A3: R is sufficiently small and w^s is thereby sufficiently large such that

\beta R < 1

\beta w^s > h

A4: w^u is sufficiently small such that

w^u < \hat{b}(1/\beta - R)

implying that

\beta(w^u + \hat{b}R) < \hat{b}

Note that:

(1) this assumption can be expressed as an assumption on the parameters:

w^u < (1 - \beta R)(hR\theta - w^s)/[\beta R\theta - 1]

(2) A4 implies that

\beta R < 1

Assumptions A1 - A4 assure that the dynamical system is characterized by 2

stable steady states:

b^L = \frac{\beta w^u}{1 - \beta R}

i.e., b^L = \beta(b^L R + w^u)

b^H = \frac{\beta(w^s - hR)}{1 - \beta R}

i.e., b^H = \beta((b^H - h)R + w^s)

and a threshold unstable steady state

b^T = \frac{\beta(w^s - h\theta R)}{1 - \beta\theta R}

i.e., b^T = \beta((b^T - h)\theta R + w^s)