

differential equation full notes { mhtcet }

1. **Evaluate the derivatives:** $dx/dt = 4(2) + 3 = 11$ and $dy/dt = 2(2) - 2 = 2$
2. **Find the derivative of y with respect to x:** $dy/dx = (2) / (11) = 2/11$

Hand-Drawn Plot

Imagine a plot of the parametric curve $x(t) = 2t^2 + 3t + 1$ and $y(t) = t^2 - 2t + 1$. At $t = 2$, the curve has a slope of $2/11$, which represents the instantaneous rate of change of y with respect to x .

Code Sample

In Python, we can use the sympy library to calculate the derivative of a parametric function:

```
import sympy as sp
```

```
t = sp.symbols('t')
```

```
x = 2*t**2 + 3*t + 1
```

```
y = t**2 - 2*t + 1
```

```
dxdt = sp.diff(x, t)
```

```
dydt = sp.diff(y, t)
```

```
dydx = dydt / dxdt
```

```
print(dydx)
```

This code will output the derivative of y with respect to x as a function of t .

Key Takeaways

- Parametric functions define a curve in terms of a parameter (usually time).
- The derivative of a parametric function represents the instantaneous rate of change of the curve.
- To calculate the derivative, use the chain rule and divide the derivative of y with respect to t by the derivative of x with respect to t .

Logarithmic Differentiation: Unlocking the Power of Complex Functions

Imagine you're trying to differentiate a complex function, but it's like trying to untangle a knot - it's frustrating and seems impossible. That's where logarithmic differentiation comes in, a powerful technique that helps you find the derivative of complicated functions with ease.

The Basic Idea

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Page 4 of 6