

# Friction

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## 1 Mathematical Induction

Apart from normal methods that we are using to solve **mathematical equations or expressions** there exists some other methods.

**Mathematical Induction** can be used as a method to show that a mathematical expression or a equation is true for all the positive integer  $\mathbb{R}^+$  values.

In this chapter we are comprehensively studying **mathematical induction and it's uses**.

Now let us consider the below mentioned example.

Let  $(xy)^n = x^n y^n$  be a mathematical expression which can be represented by  $P_n$  where  $n \in \mathbb{R}^+$ . Here  $x$  and  $y$  are real numbers.

Hence,

when  $n=1$ ;  $(xy)^1 = xy$  is represented by  $P_1$

when  $n=2$ ;  $(xy)^2 = x^2 y^2$  is represented by  $P_2$

when  $n=3$ ;  $(xy)^3 = x^3 y^3$  is represented by  $P_3$

.....

From general understanding of multiplication and power rules for real numbers, it's obvious tha the above  $P_1, P_2, P_3$  are true. But for all infinite number of  $n$  we can't prove that  $P_n$  from the above method. Therefore **mathematical induction** can be used in such circumstances.

## 2 Mathematical Induction Concept

Let us consider an expression consists of the  $n$  variable which can be represented by  $P_n$ . Now let us consider the following points.

i)  $P_1$  is true in the above statement.

ii) When  $k$  is a positive integer, if  $P_k$  is true then  $P_{k+1}$  is also true. This can be written as  $P_k \implies P_{k+1}$