

$$\frac{x - x_0}{t} = v_{0x} + \frac{1}{2} a_x t$$

$$\Rightarrow x - x_0 = t \left(v_{0x} + \frac{1}{2} a_x t \right)$$

$x - x_0 = v_{0x}t + \frac{1}{2} a_x t^2 \dots \dots \dots (1.4)$	Working formula
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Derivation of 3rd kinematic equation:

To relate displacement, acceleration, initial velocity and final velocity, we should find the time from equation (1.1) as

$$t = \frac{v_x - v_{0x}}{a_x} \dots \dots \dots (1.5)$$

Substituting above value of time 't' in eq.(1.4), we get

$$x - x_0 = v_{0x}t + \frac{1}{2} a_x t^2$$

$$\Rightarrow x - x_0 = v_{0x} \left(\frac{v_x - v_{0x}}{a_x} \right) + \frac{1}{2} a_x \left(\frac{v_x - v_{0x}}{a_x} \right)^2$$

$$\Rightarrow x - x_0 = \frac{v_{0x}v_x}{a_x} - \frac{v_{0x}^2}{a_x} + \frac{1}{2} a_x \left(\frac{v_x^2 - v_{0x}^2 - 2v_{0x}v_x}{a_x^2} \right)$$

$$\Rightarrow x - x_0 = \frac{2v_{0x}v_x - 2v_{0x}^2 + v_x^2 + v_{0x}^2 - 2v_{0x}v_x}{2a_x}$$

$$\Rightarrow 2a_x(x - x_0) = v_x^2 - v_{0x}^2$$

$v_x^2 = v_{0x}^2 + 2a_x(x - x_0) \dots \dots \dots (1.6)$	Working formula
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The above eq.(1.1),(1.4) and (1.6) can be resolved in to three sets of equations to describe the motion along the three Cartesian directions as

$v_x = v_{0x} + a_x t;$	$v_y = v_{0y} + a_y t;$	$v_z = v_{0z} + a_z t;$
$(x - x_0) = v_{0x}t + \frac{1}{2} a_x t^2;$	$(y - y_0) = v_{0y}t + \frac{1}{2} a_y t^2;$	$(z - z_0) = v_{0z}t + \frac{1}{2} a_z t^2;$
$v_x^2 = v_{0x}^2 + 2a_x(x - x_0);$	$v_y^2 = v_{0y}^2 + 2a_y(y - y_0);$	$v_z^2 = v_{0z}^2 + 2a_z(z - z_0);$

Best of luck