

1. find the partial derivative with respect to each variable, for $f(x, y) = e^{xy^2}$:

$$\frac{\partial f}{\partial x} = e^{xy^2} \cdot \frac{\partial}{\partial x} xy^2 = e^{xy^2} \cdot y^2 = y^2 e^{xy^2}$$

$$\frac{\partial f}{\partial y} = e^{xy^2} \cdot \frac{\partial}{\partial y} xy^2 = e^{xy^2} \cdot x \cdot 2y = 2xy e^{xy^2}$$

2. find the partial derivative with respect to each variable, for $f(x, y, z) = y \sin(xz) - z \ln(xy)$:

$$\frac{\partial f}{\partial x} = y \cdot \cos(xz) \cdot \frac{\partial}{\partial x} (xz) - z \cdot \frac{1}{xy} \cdot \frac{\partial}{\partial x} (xy) =$$

$$y \cos(xz) \cdot z - z \cdot \frac{1}{xy} \cdot y = yz \cos(xz) - \frac{z}{x}$$

$$\frac{\partial f}{\partial y} = \sin(xz) - z \cdot \frac{1}{xy} \cdot \frac{\partial}{\partial y} (xy) = \sin(xz) - \frac{z}{xy} \cdot x =$$

$$\sin(xz) - \frac{z}{y}$$

$$\frac{\partial f}{\partial z} = y \cdot \cos(xz) \cdot \frac{\partial}{\partial z} (xz) - \ln(xy) = y \cdot \cos(xz) \cdot x - \ln(xy) =$$

$$xy \cos(xz) - \ln(xy)$$

3. integrate :

$$\int_0^2 \int_0^{4-2y} x+y \, dx \, dy = \int_0^2 \left[\frac{x^2}{2} + xy \right]_{x=0}^{x=4-2y} dy =$$

$$\int_0^2 \left[\frac{1}{2} (4-2y)^2 + y(4-2y) \right] - \left[\frac{1}{2} \cdot 0 + 0 \cdot y \right] dy = \int_0^2 \frac{1}{2} (16 - 16y + 4y^2) + 4y - 2y^2 dy$$

$$= \int_0^2 8 - 8y + 2y^2 + 4y - 2y^2 dy = \int_0^2 8 - 4y dy = \left[8y - 4 \cdot \frac{1}{2} y^2 \right]_0^2 =$$

$$\left[8y - 2y^2 \right]_0^2 = 8 \cdot 2 - 2 \cdot 2^2 - (8 \cdot 0 - 2 \cdot 0^2) = 16 - 8 = 8$$