

Topic I—Algebra

1.1	The n^{th} term of an arithmetic sequence The sum of n terms of an arithmetic sequence The n^{th} term of a geometric sequence The sum of n terms of a finite geometric sequence The sum of an infinite geometric sequence	$u_n = u_1 + (n-1)d$ $S_n = \frac{n}{2}(2u_1 + (n-1)d) = \frac{n}{2}(u_1 + u_n)$ $u_n = u_1 r^{n-1}$ $S_n = \frac{u_1(r^n - 1)}{r - 1} = \frac{u_1(1 - r^n)}{1 - r}, \quad r \neq 1$ $S_\infty = \frac{u_1}{1 - r}, \quad r < 1$
1.2	Exponents and logarithms Laws of logarithms Change of base	$a^x = b \Leftrightarrow x = \log_a b$ $\log_c a + \log_c b = \log_c ab$ $\log_c a - \log_c b = \log_c \frac{a}{b}$ $\log_c a^r = r \log_c a$ $\log_b a = \frac{\log_c a}{\log_c b}$
1.3	Binomial coefficient Binomial theorem	$\binom{n}{r} = \frac{n!}{r!(n-r)!}$ $(a+b)^n = a^n + \binom{n}{1}a^{n-1}b + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n$