

Transformations on Conic Sections

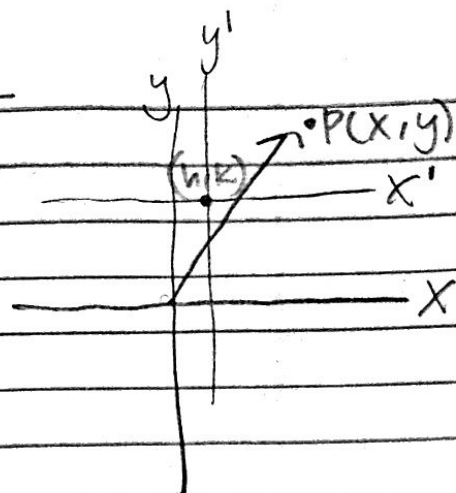
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$$x' = x - h$$

$$y' = y - k$$

$$x = x' + h$$

$$y = y' + k$$



eliminating 2nd degree terms means eliminating things to the 1st power

ex) $x \rightarrow$ 1st deg

$x^2 \rightarrow$ 2nd deg

$xy \rightarrow$ 2nd deg

constant = everything w/o an x or y

If an xy term in final eqn $\rightarrow$ means rotated

$$\begin{aligned} x &= \cos \theta x' + \sin \theta y' \\ y &= -\sin \theta x' + \cos \theta y' \end{aligned}$$

points rotate (θ), axes rotate ($-\theta$)

after plug in and get simplified eqn, it is on the $x' y'$ axes, draw on rotated $x' y'$ axes

can transform pts from $x' y'$ axis back to $x y$ w/ same equations

If need to transform a line back, use

$$\begin{aligned} x' &= \cos \theta x - \sin \theta y \\ y' &= \sin \theta x + \cos \theta y \end{aligned}$$