

★ Displacement current :-

For static electro magnetic field, by Ampere's circuital law:

$$\nabla \times \vec{H} = \vec{J} \quad \text{--- (1)}$$

taking divergence

$$\nabla \cdot (\nabla \times \vec{H}) = \nabla \cdot \vec{J}$$

but ∇ Product of any vector is zero.

$$\therefore \nabla \cdot (\nabla \times \vec{H}) = \nabla \cdot \vec{J} = 0 \quad \text{--- (2)}$$

\therefore Continuity eqⁿ says that.

$$\nabla \cdot \vec{J} = -\frac{\partial \rho}{\partial t}$$

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eqⁿ (2) & (3) are incompatible for time varying fields.

$$\therefore \nabla \times \vec{H} = \vec{J} + \vec{J}_d$$

(adding of new component)

$$\therefore \nabla \cdot (\nabla \times \vec{H}) = \nabla \cdot \vec{J} + \nabla \cdot \vec{J}_d = 0$$

by applying continuity eqⁿ

$$\nabla \cdot \vec{J}_d = -\nabla \cdot \vec{J} = \frac{\partial \rho}{\partial t} \rightarrow \text{apply Stokes's Gauss}$$

$$\therefore \nabla \cdot \vec{J}_d = \frac{\partial (\nabla \cdot \vec{D})}{\partial t}$$